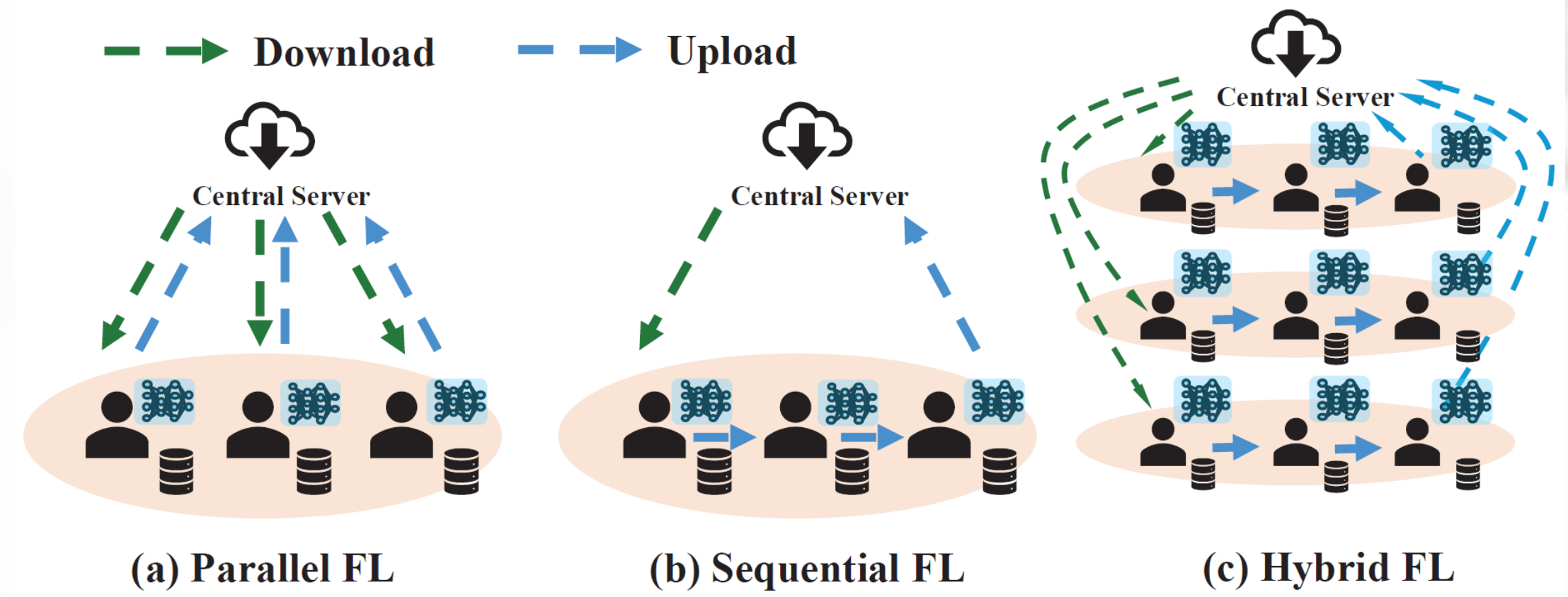


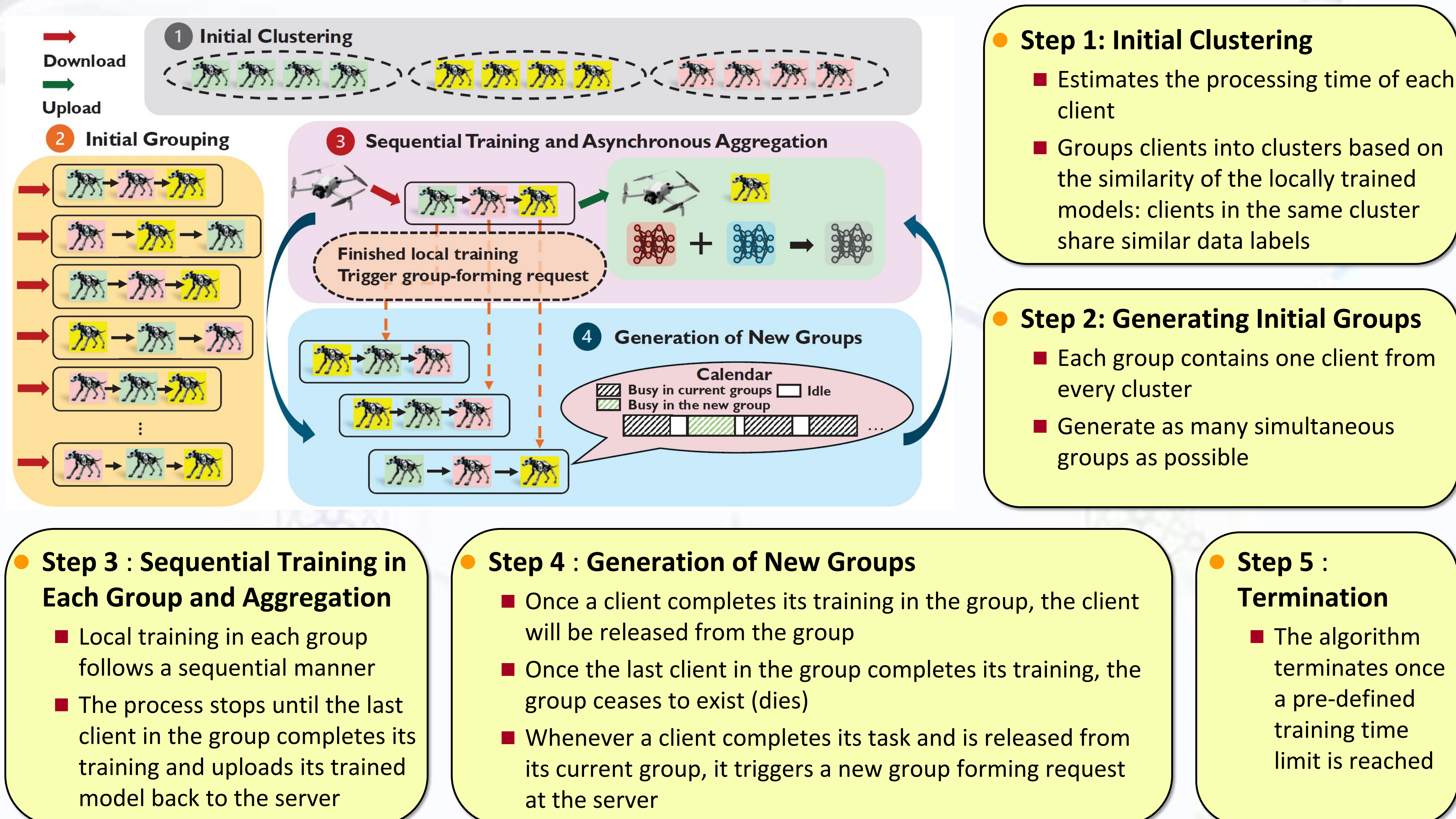
## Background



- **Parallel FL**
  - **Pros:** Parallelism shorten the round duration
  - **Cons:** Performance degraded by small-scale and heterogenous clients' local datasets
- **Sequential FL**
  - **Pros:** Each client's information is captured without destructive cancellation
  - **Cons:** There is only one client busy training at any time
- **Hybrid FL**
  - **Pros:** General form for both parallel and sequential FL
  - **Cons:** Each group still inherits client idleness

**Problem: Accelerate Hybrid FL**

## FedHusky: Overview



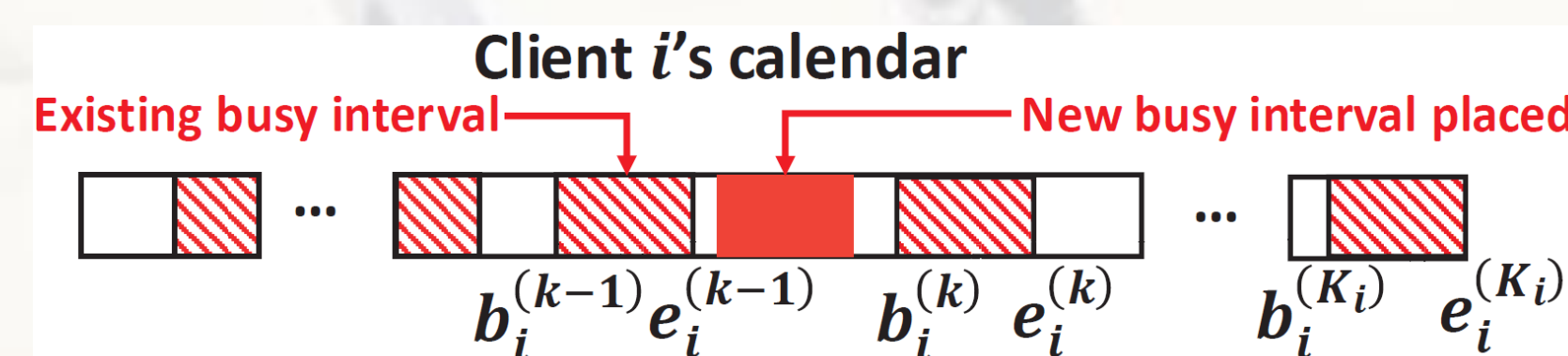
- **Step 1: Initial Clustering**
  - Estimates the processing time of each client
  - Groups clients into clusters based on the similarity of the locally trained models: clients in the same cluster share similar data labels
- **Step 2: Generating Initial Groups**
  - Each group contains one client from every cluster
  - Generate as many simultaneous groups as possible
- **Step 3: Sequential Training in Each Group and Aggregation**
  - Local training in each group follows a sequential manner
  - The process stops until the last client in the group completes its training and uploads its trained model back to the server
- **Step 4: Generation of New Groups**
  - Once a client completes its training in the group, the client will be released from the group
  - Once the last client in the group completes its training, the group ceases to exist (dies)
  - Whenever a client completes its task and is released from its current group, it triggers a new group forming request at the server
- **Step 5: Termination**
  - The algorithm terminates once a pre-defined training time limit is reached

## FedHusky: Step 1

- Determine **how many** clusters will be formed
    - Too few clusters may put dissimilar clients in the same group
    - Too many clusters may excessively fragment the data labels
- Gap Statistic and K-means algorithms**
- 
- **Rebalance Step**
    - We should have a cluster size of either  $\lfloor \frac{N}{C} \rfloor$  or  $\lceil \frac{N}{C} \rceil$
    - For a cluster with more than  $\lfloor \frac{N}{C} \rfloor$  clients, the server discards the "farthest" clients and reassigns them to the cluster that is "nearest" that currently has fewer clients than  $\lfloor \frac{N}{C} \rfloor$

## FedHusky: Step 2

- **Goal:** Form as many groups as possible by allowing a client to participate in as many groups as possible, if it is **not double-booked** at the same time
- The server iteratively considers each client from 1 to  $N$  as the first member of a potential group**
- Generate the **FIRST** group
  - First spot (client#1), rest spots (Rest  $C - 1$  clusters randomly pick 1 for each)
  - Each client maintains a **calendar**  $\mathcal{B}_i = \{[b_i^{(k)}, e_i^{(k)}], k = 1, 2, \dots\}$  recording its busy interval
- Generate the **SECOND** group
  - First spot (client#2)
  - Rest spots: Need to model an optimization problem to ensure no double-booking
  - Decision variables
    - ◆ **Client selection:**  $x_i$ , **position placement:**  $y_{i \rightarrow p}$ , **starting time of position  $p$ :**  $h[p]$ , **starting time of client  $i$ :**  $s_i$ , **calendar gap insertion:**  $z_i^{(k)}$
  - Constraints
    - ◆ Each cluster selects one client, each position places one client, each client placed at one spot, new busy interval can be inserted into one gap in calendar
  - Objective
    - ◆ Define a busy ratio of client  $i$ :  $\theta_i$ . If  $i$  is not selected in group 1:  $\theta_i = 0$ . If  $i$  is selected in group 1:  $\theta_i = (e_i^{(1)} - b_i^{(1)})/T$
    - ◆ OPT-2:  $\max \min \theta_i + \Delta_i x_i / T$
  - After solving, selected clients for group 2 update each of their calendars
- Generate the  **$i$ -th** group
  - Solve OPT- $i$
  - For OPT- $i$ 
    - ◆ If optimal: update calendars, group formed
    - ◆ If infeasible: Move on to OPT- $(i + 1)$
  - After solving OPT- $N$ , step 2 completed



## FedHusky: Step 3

- **Sequential Training**
  - Server transmits the global to the first client in the group
  - After finished training, the first client passes the model to the next client
  - Last client completes its training and uploads the final model back to the server
  - Wireless relay
    - ◆ Ad Hoc networking or Use server as a relay, whichever is faster
- **Asynchronous Aggregation**
  - Whenever the last client in a group completes its training, it sends its model to the server for aggregation
  - Use an aggregation coefficient so that larger gap, smaller aggregation weight

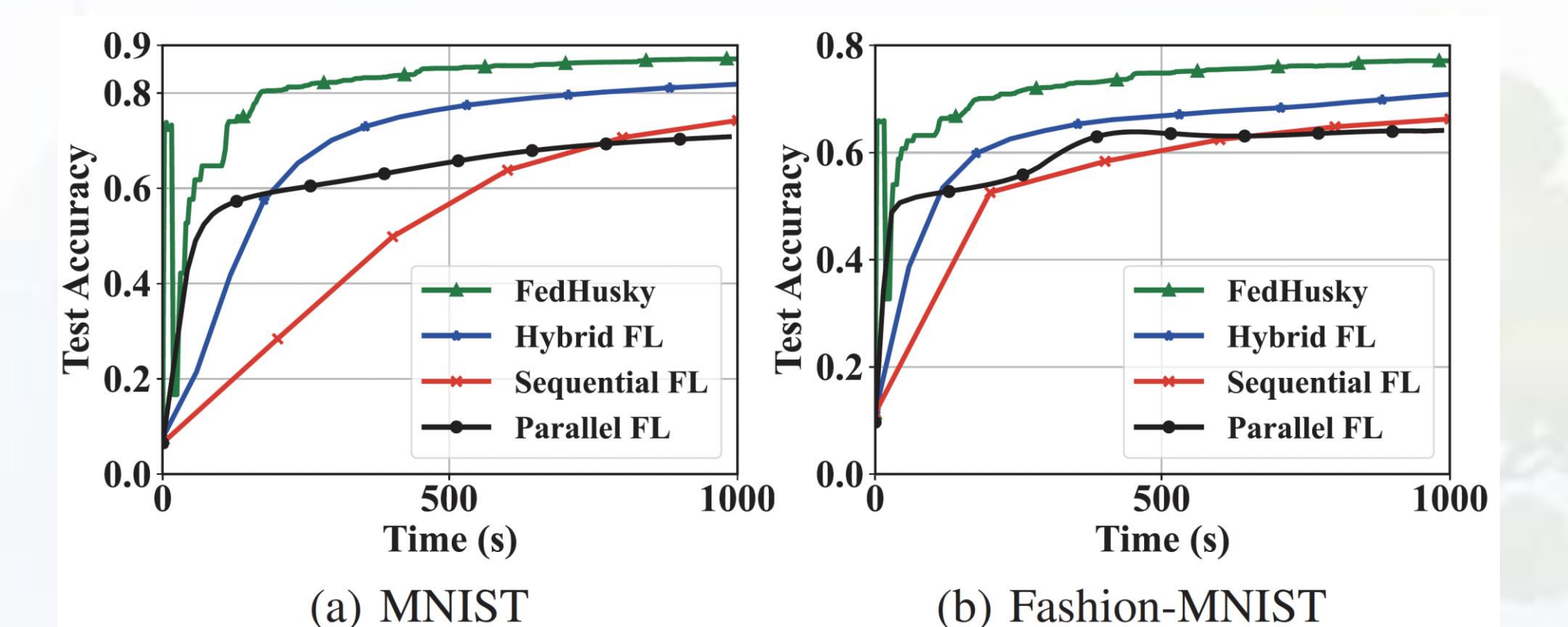
## FedHusky: Step 4

- Each generated group is used only once
  - When a client finishes training and relaying, it is released
  - When the last client finishes, the group dies
- Solving new optimization problem OPT- $k$ ,  $k > N$ 
  - No need the specify the first position of the group:  $x_2 = 1, y_{2 \rightarrow 1}$
  - $t_0$  is shifted to the current wall-clock time:  $h[1] = t_0$
  - If there is a feasible solution of OPT- $k$ , a new group formed, otherwise, no new group
- Server waits until the next client notification arrives and then starts the same process for OPT- $(k + 1)$

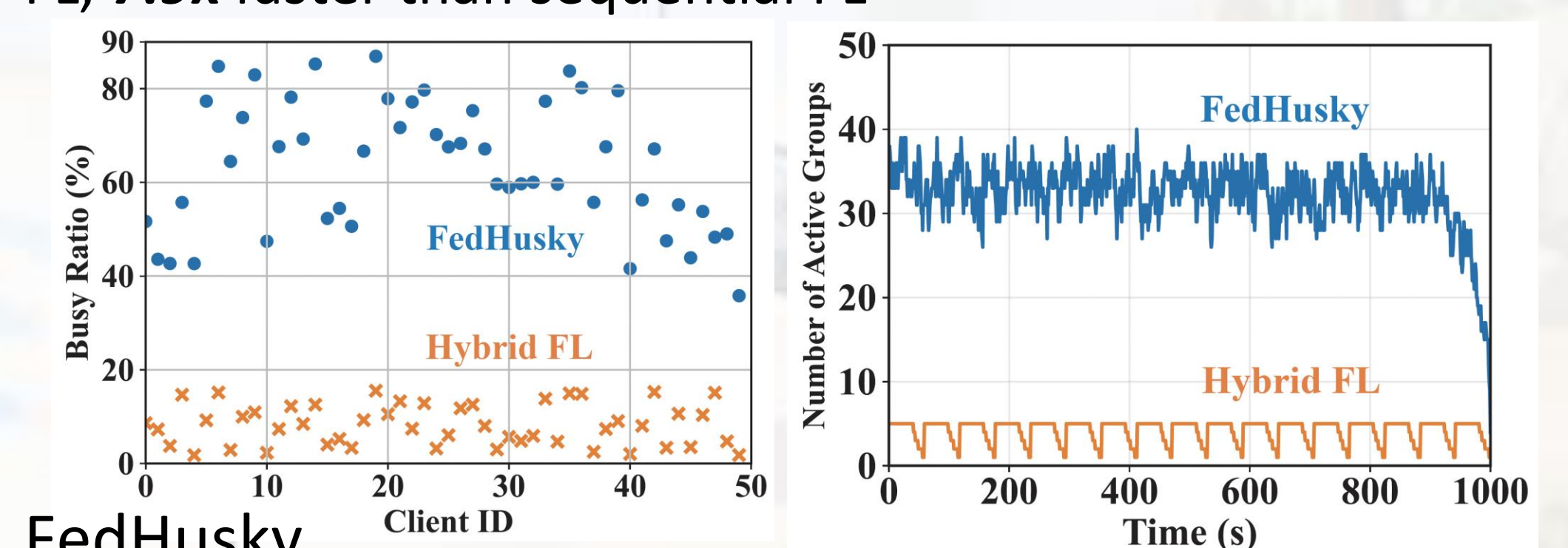
## Publication

F. Zhou, Y. Shi, W. Lou, and Y. T. Hou, "FedHusky: Accelerating Hybrid Federated Learning with Client Hopping," in Proc. International Symposium on Modeling and Optimization in Mobile, Adhoc, and Wireless Networks (WiOpt), Columbus, Ohio, USA, June 2026.

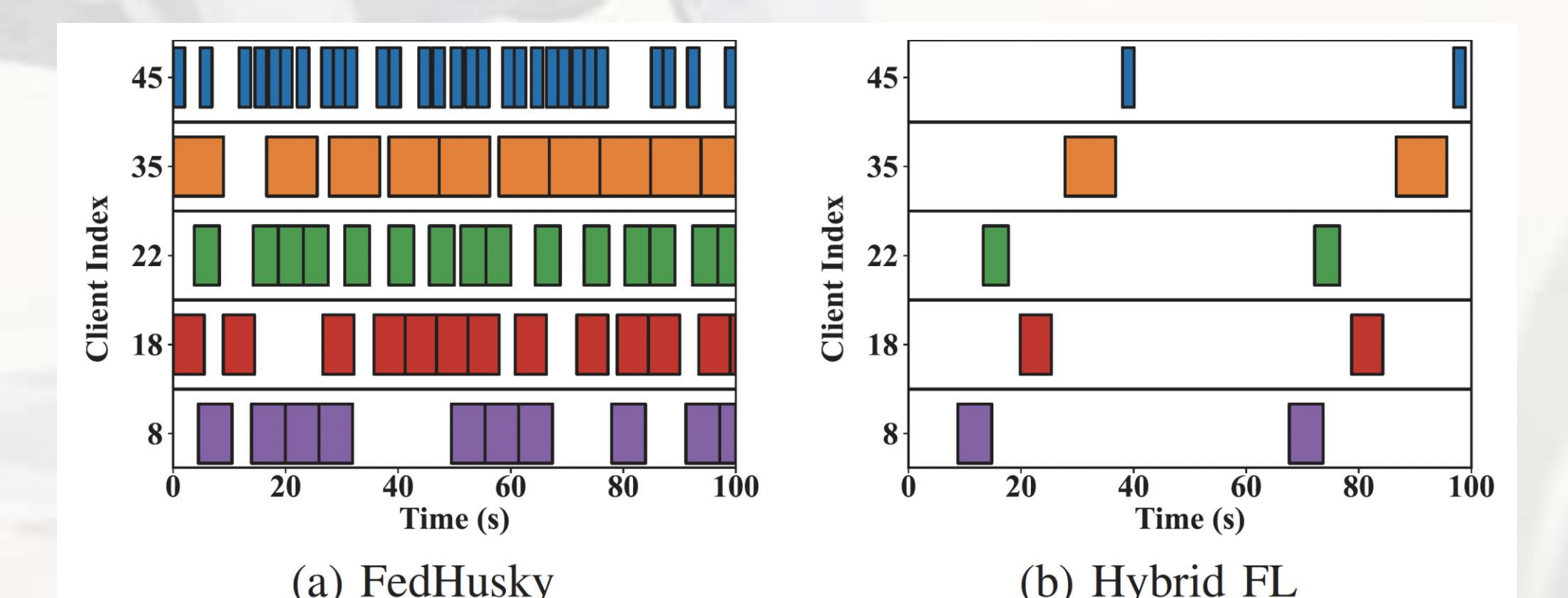
## Results: Case Study



- 80% accuracy: FedHusky converges **5.9x** faster than hybrid FL, **7.9x** faster than sequential FL



- FedHusky
  - Busy ratio varies from 35.8% to 86.9% over the 50 clients, with the average ratio being 63.4%
- Hybrid FL
  - Busy ratio varies from 1.8% to 15.5%, with the average ratio being 8.2%



- Examine the calendar of each individual client
  - Each client under FedHusky clearly **works much harder** (more efficiently) than it works under hybrid FL